

Immink Codes for Phase Change Memory

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June 15, 2017

Figure 1 by Shannon

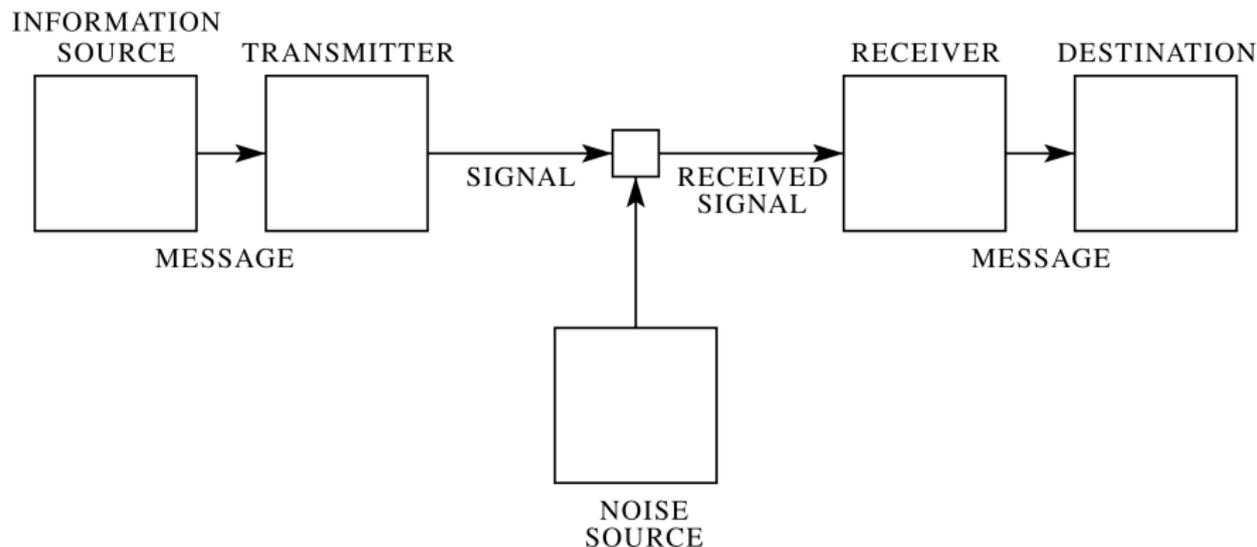


Fig. 1—Schematic diagram of a general communication system.

C. Shannon, "A mathematical theory of communication", The Bell system Technical Journal, vol. 27, pp.379–423, 623–656, July, October, 1948.

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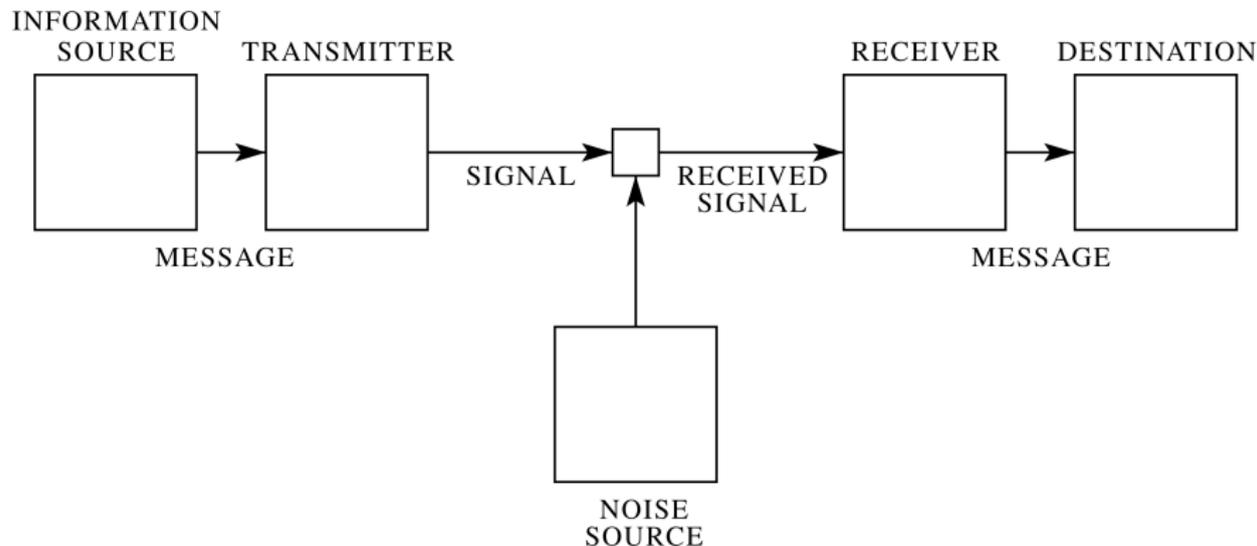


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K. Immink's talk at Almaden research center, CA, USA.

Figure 1 by Shannon(in Japanese)

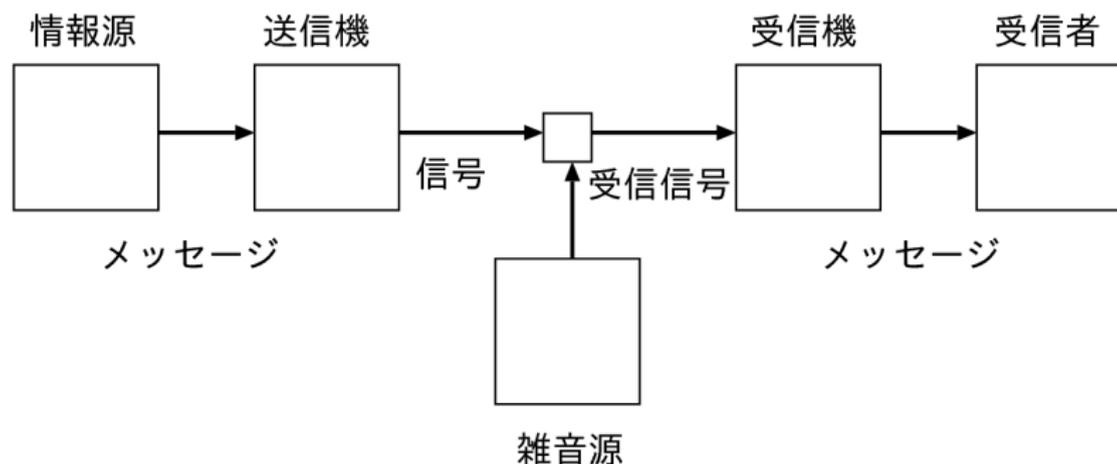


Figure: 一般的な通信路の概念図

C. Shannon, "A mathematical theory of communication", The Bell system Technical Journal, vol. 27, pp.379–423, 623–656, July, October, 1948.

Digital Communication System

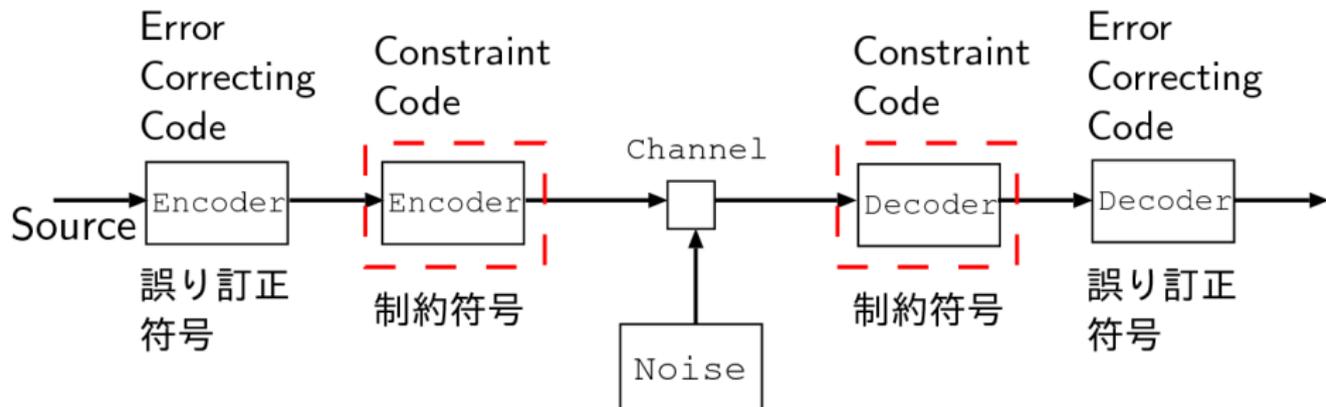
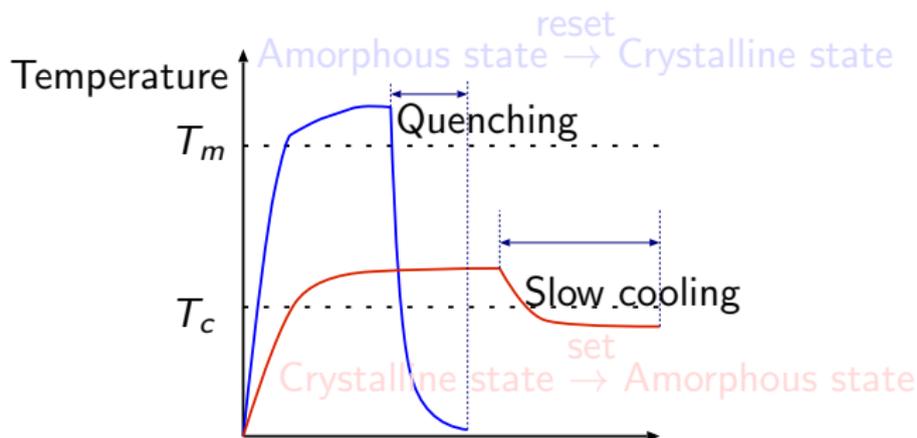


Figure: Schematic Diagram of Digital Communication System

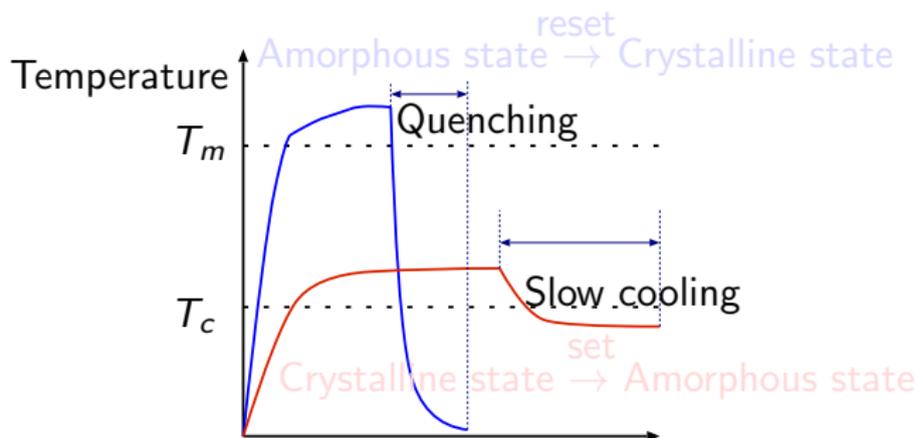
Introduction

- Phase change memory: a non volatile semiconductor memory to which we can store digital data almost freely (no restriction, i.e., the number of rewrites of flash memory cells is almost ∞ , etc).
- The phase (or state) of a cell of PCM is changed by heating; quick heating and cooling (amorphous to crystalline state, **reset** operation), slow heating and cooling (crystalline to amorphous state, **set** operation)
- Amorphous state: High resistance, 1, Crystalline state: Low resistance, 0



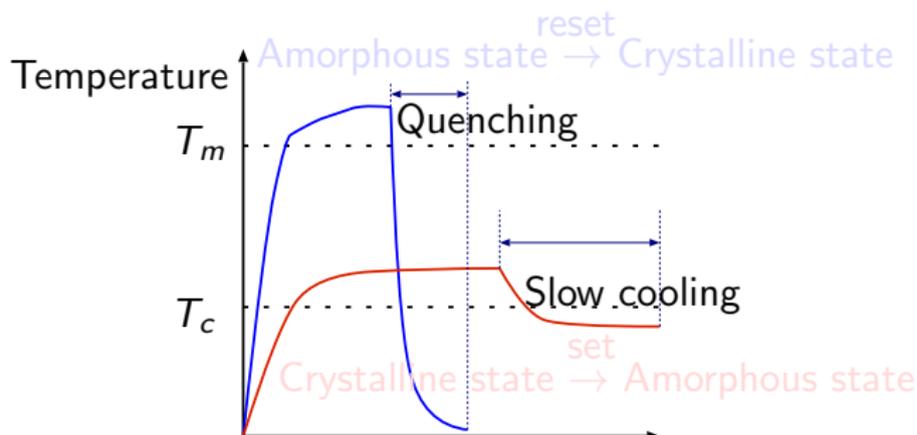
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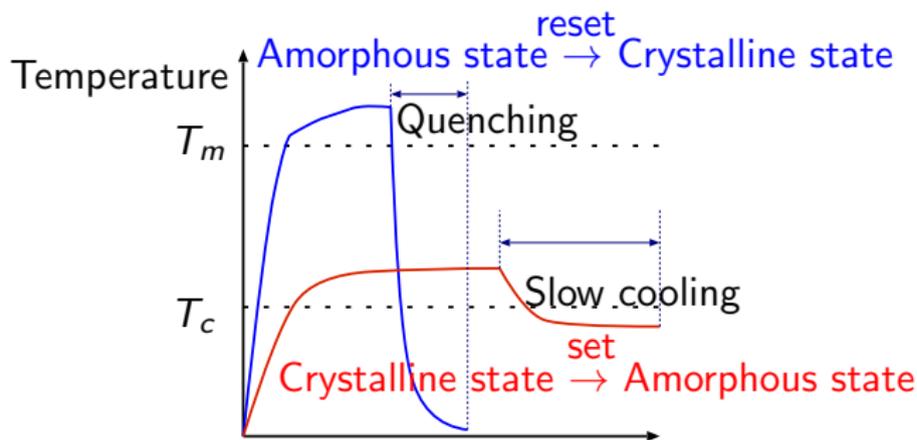
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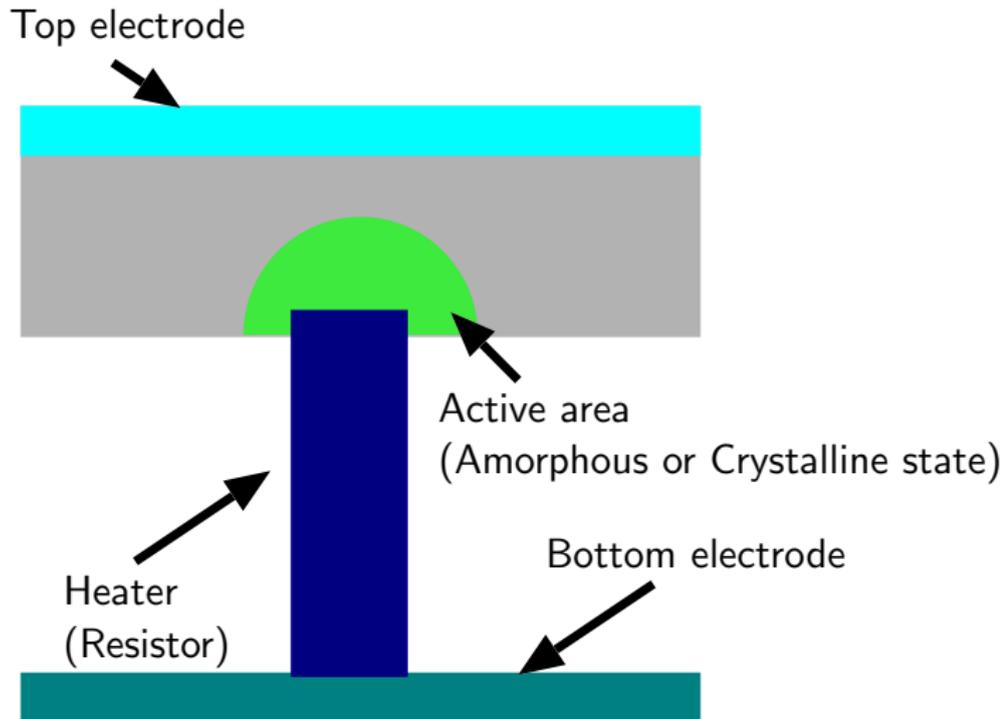


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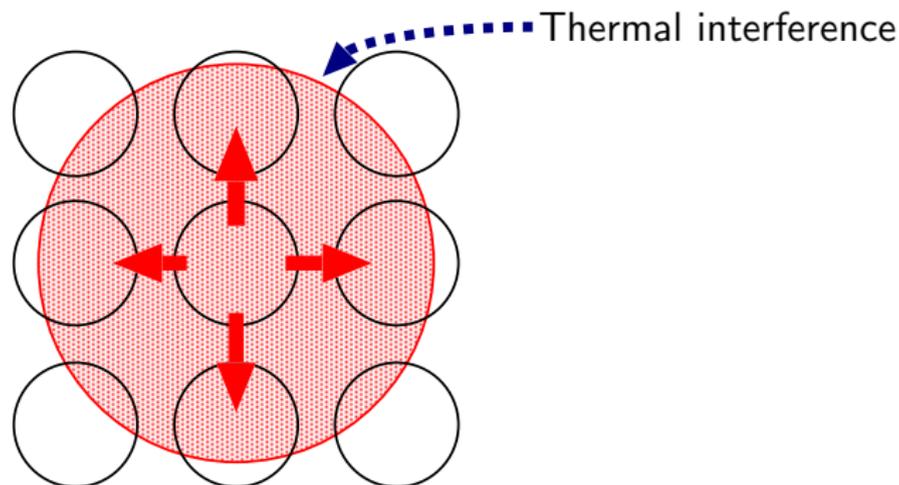
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Cell Structure of PCM

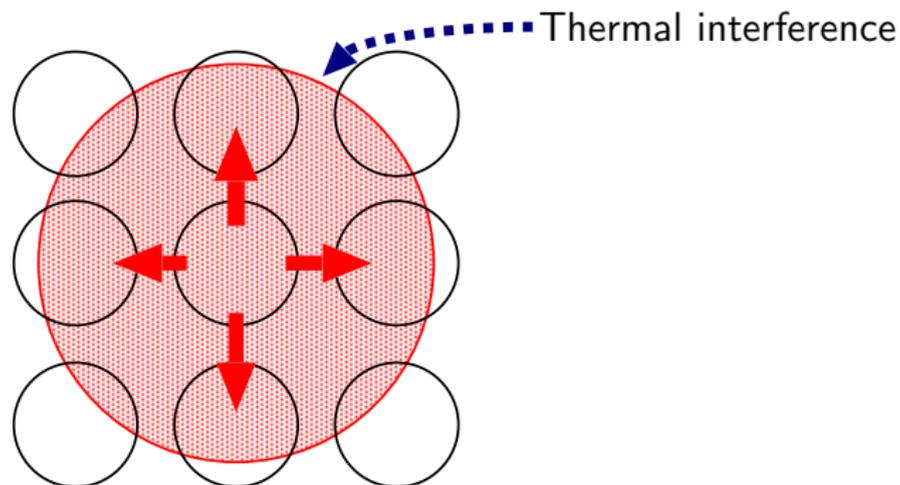


Cross talk problem, set and reset operation



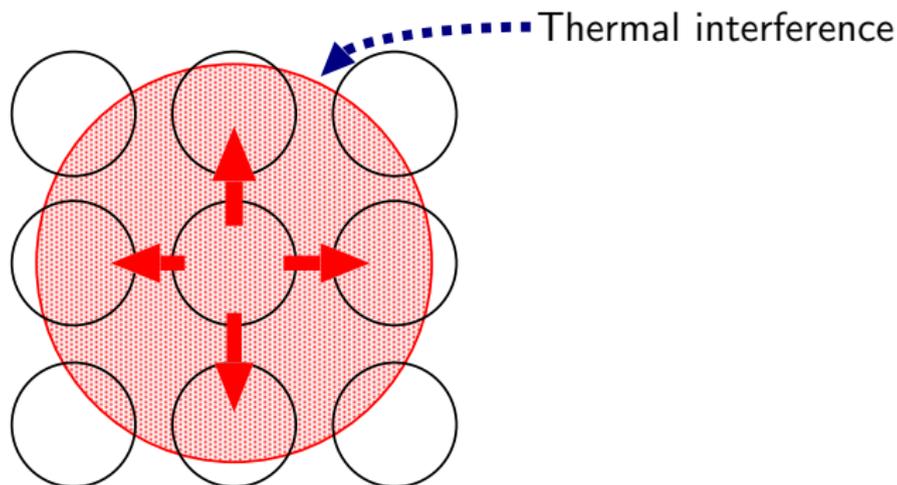
- The reset operation causes a strong thermal interference.
- A 2-dimensional constraint is needed but the capacity of the 2-dimensional constraint is small in many cases.
- We construct a 1-dimensional constraint code and evaluate it by computer simulation.

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Our Code

- 1 K. Cai constructed an efficient code for k -constraint where $k = 3$ by using Imrink coding [K.Cai, 2014].
- 2 We also construct a code for $k = 3$ to avoid long runs of zeros.
- 3 When $k = 3$, left ends of k constrained sequences are

1, ,01, 001, 0001.

- 4 Let s_1, s_2, s_3 and s_4 be numbers of states corresponding to the above sequences, respectively.
- 5 Then apply the Imrink coding.
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Immink coding for $d = 1$ constraint

- n : code length
- E_{ab} : set of constrained sequences of length n starting with symbol a and terminating with symbol b .

- 1 Find positive integers r_1 and r_2 satisfying the following inequalities:

$$(r_1 + r_2)|E_{00}| + r_1|E_{01}| \geq r_1 2^m \quad (1)$$

$$(r_1 + r_2)(|E_{00}| + |E_{10}|) + r_1(|E_{01}| + |E_{11}|) \geq (r_1 + r_2) 2^m \quad (2)$$

- 2 If we can find the r_1 and r_2 , then according to the we can construct an encoding rule and a corresponding decoding rule for the $d = 1$ constraint.
- 3 Note: When we construct these rules, we can almost ignore constrained patterns and can concentrate only on the numbers of patterns, $|E_{00}|, \dots$

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Step 1

- If we can find positive integers s_1, s_2, s_3 and s_4 and m satisfying the following equations, we can construct a code by Immink coding [K. Cai 2014].

$$(s_1 + s_2 + s_3 + s_4)|C_{1\dots 1}| \geq s_1 2^m$$

$$(s_1 + s_2 + s_3 + s_4)(|C_{1\dots 1}| + |C_{01\dots 1}|) \geq (s_1 + s_2)2^m$$

$$(s_1 + s_2 + s_3 + s_4)(|C_{1\dots 1}| + |C_{01\dots 1}| + |C_{001\dots 1}|) \\ + (s_1 + s_2 + s_3)(|C_{1\dots 10}| + |C_{01\dots 10}|) \geq (s_1 + s_2 + s_3)2^m$$

$$(s_1 + s_2 + s_3 + s_4)(|C_{1\dots 1}| + |C_{01\dots 1}| + |C_{001\dots 1}| + |C_{0001\dots 1}|) \\ + (s_1 + s_2 + s_3)(|C_{1\dots 10}| + |C_{01\dots 10}|) \geq (s_1 + s_2 + s_3 + s_4)2^m$$

where $C_{\alpha\dots\beta}$ means a set of constrained sequences having prefix α and postfix β .

Step 2

- The previous inequalities mainly concerns the numbers of code words.
- If (the left hand side) $>$ (the right hand side), then we can discard code words in $C_{\alpha\dots\beta}$, for example,

$$(s_1 + s_2 + s_3 + s_4)|C_{1\dots 1}| > s_1 2^m$$

- If the frequency of 000 is small then the probability of the reset changes may be small.
- We discard sequences containing many consecutive zeros, e.g., 0001, 1000, 000101000.
- We accept a code with low code rate and then get the freedom of adjustment of the resulting code.
- This adjustment or tuning is possible with almost no cost thanks to the Imminck coding. So we can construct and try many different codes easily.

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Result 1 by Li Bojun[2017]

N : the total number of cells

$N_{1 \Rightarrow 0}$: the number of reset changes

P_{reset} : the frequency of reset changes

$$P_{reset} = \frac{N_{1 \Rightarrow 0}}{N}$$

Table: P_{reset}

Length	Cells reset	P_{reset}
90	20535	0.2281
900	209592	0.2329
1800	419471	0.2330

where 'length' means the length of blocks of encoded cells and random data were written on the cells 1000 times.

Result 2 by Li Bojun[2017]

	No coded	K. Cai	K. Cai	Proposed
k	-	$k = 1$	$k = 3$	$k = 3$
Capacity	1	0.6942	0.9468	0.94468
Code length	-	13	18	9
Code rate	1	0.6923	0.9444	0.8889
P_{reset}	0.5	0.2773	0.4337	0.2230
R	0%	44.54%	13.26%	53.40%

where R is a rate of decrease in the frequency of reset changes and is

$$R = \frac{(P_{reset} \text{ of No Coded}) - P_{reset}}{P_{reset} \text{ of No Coded}} = \frac{0.5 - P_{reset}}{0.5}$$

- R of our code is the best among the above codes.
- The code rate of our code is lower than that of Cai's $k = 3$ code but our code is better than Cai's $k = 1$ code.
- Our code reduces the frequency of reset changes with relatively high code rate.

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New PCM

- There are new PCM technologies with new materials and with a new physical phenomenon, for example, interfacial phase change memory (IPCM).
- IPCM uses only the crystalline state and a laser beam changes its phase (resistance). There is no thermal interference among cells in IPCM.
- We must find a new constraint for IPCM.

Simpson, R.E.; P. Fons; A. V. Kolobov; T. Fukaya; et al. "Interfacial phase-change memory". Nature Nanotechnology, pp 501–505, July, 2011.

Conclusion

- Thermal interference of PCM.
- k -constraint for PCM.
- Immink coding for PCM.
- If we use the Immink coding, it is easy to tune or adjust the resulting code so that it has a good performance for PCM.

Reference

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