# A conceptual framework for structural design and optimization using quantum computing 

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## Quantum Computing at TU Delft



## Quantum Computing at DIAM

- Bachelor projects
- M. v.d. Lans: Multi-search Groover, Q-add/sub
- M. Looman: Q-add with simulated quantum errors
- R. Nugteren: Q-mul for Noisy Intermediate-Scale Quantum (NISQ)
- S. v.d. Linde: Posit arithmetics
- O. Ubbes: Quantum Linear Solver Algorithm (QLSA)
- T. Driebergen: Posit arithmetics for QC
- M. Schalkers (internship at TNO): LibKet, unitary decomposition
- Collaborations and support:
- TNO, TU Delft Quantum \& Computer Engineering, SURFsara, 4TU.CEE


## Outlook

- Basic Concepts of quantum computing
- Quantum bits, registers, gates, and algorithms
- Quantum-accelerated design optimization
- A conceptual framework
- Practical aspects of quantum computing
- SDKs and good practices
- Conclusion
entanglement paradox teleportation
classical measurement Bob

Basic concepts of quantum computing

## QUANTUM BITS

## From bits to quantum bits

- Classical bits
- Quantum bits (qubits)



## From bits to quantum bits

- Classical bits
- Quantum bits (qubits)



## The Bloch sphere

- Quantum state

$$
|\psi\rangle=\cos \frac{\theta}{2} \cdot|0\rangle+e^{i \varphi} \cdot \sin \frac{\theta}{2} \cdot|1\rangle
$$

- Basis states $|0\rangle$ and $|1\rangle$
- Latitude $\theta \in[0, \pi]$
- Longitude $\varphi \in[0,2 \pi)$



## The Bloch sphere, cont'd

- $\theta=0$ implies
$|\psi\rangle=1 \cdot|0\rangle+e^{i \varphi} \cdot 0 \cdot|1\rangle=|0\rangle$
- $\theta=\pi$ implies
$|\psi\rangle=0 \cdot|0\rangle+e^{i \varphi} \cdot 1 \cdot|1\rangle=|1\rangle$
- Poles represent classical bits



## The Bloch sphere, cont'd

- $\theta=\frac{\pi}{2}$ and $\varphi=0$ implies

$$
|\psi\rangle=\frac{1}{\sqrt{2}} \cdot|0\rangle+\frac{e^{i 0}}{\sqrt{2}} \cdot|1\rangle=\frac{|0\rangle+|1\rangle}{\sqrt{2}}
$$

- $\theta=\frac{\pi}{2}$ and $\varphi=\pi$ implies
$|\psi\rangle=\frac{1}{\sqrt{2}} \cdot|0\rangle+\frac{e^{i \pi}}{\sqrt{2}} \cdot|1\rangle=\frac{|0\rangle-|1\rangle}{\sqrt{2}}$



## What to do with this added value?

- Classical bits
- Quantum bits (qubits)



## Intermezzo: Schrödinger's cat



## Intermezzo: Schrödinger's cat, cont'd

- Before opening the box

$$
\begin{aligned}
& \left.\frac{1}{\sqrt{2}}|\vec{m}\rangle+\frac{1}{\sqrt{2}} \right\rvert\, \Rightarrow \\
& \text { ( }{ }^{3} \gg 0 \text { or } \Rightarrow
\end{aligned}
$$

- After opening the box


## Intermezzo: Schrödinger's cat, cont'd

- Repeating the experiment many times $50 \%$ of the cats are dead, $50 \%$ alive



## From Bloch's sphere to probabilities

- Coefficients of the basis expansion

$$
|\psi\rangle=\cos \frac{\theta}{2} \cdot|0\rangle+e^{i \varphi} \cdot \sin \frac{\theta}{2} \cdot|1\rangle
$$

represent the probability amplitude that the quantum state $|\psi\rangle$ collapses to either of the two basis states $|0\rangle$ or $|1\rangle$ upon measurement since

$$
\left|\cos \frac{\theta}{2}\right|^{2}+\left|e^{i \varphi} \cdot \sin \frac{\theta}{2}\right|^{2}=1
$$

for all latitudes $\theta \in[0, \pi]$ and longitudes $\varphi \in[0,2 \pi)$

## Life of a qubit

- Initialization into pure state $|0\rangle$



## Life of a qubit

- Initialization into pure state $|0\rangle$
- Travelling on Bloch's sphere



## Life of a qubit

- Initialization into pure state $|0\rangle$
- Travelling on Bloch's sphere
- Collapsing to either $|0\rangle$ or $|1\rangle$



## Life of a qubit

- Initialization into pure state $|0\rangle$
- Travelling on Bloch's sphere
- Collapsing to either $|0\rangle$ or $|1\rangle$
- How to describe the travelling?


Basic concepts of quantum computing

## QUANTUM GATES

## Detour to linear algebra

- Standard basis for a single-qubit state

$$
E=(|0\rangle,|1\rangle) \quad \text { with } \quad\binom{1}{0}:=|0\rangle, \quad\binom{0}{1}:=|1\rangle
$$

- Probability amplitudes (= the coefficients $|\psi\rangle$ of w.r.t. to basis $E$ )

$$
\alpha_{0}:=\cos \frac{\theta}{2}, \quad \alpha_{1}:=e^{i \varphi} \cdot \sin \frac{\theta}{2}
$$

- Coordinate representation

$$
|\psi\rangle=\alpha_{0}\binom{1}{0}+\alpha_{1}\binom{0}{1} \rightarrow[|\psi\rangle]_{E}=\binom{\alpha_{0}}{\alpha_{1}}
$$

## Detour to linear algebra, cont'd

- Initialization into pure state

$$
|\psi\rangle=1 \cdot\binom{1}{0}+0 \cdot\binom{0}{1}=\binom{1}{0}
$$



## Detour to linear algebra, cont'd

- Initialization into pure state

$$
|\psi\rangle=1 \cdot\binom{1}{0}+0 \cdot\binom{0}{1}=\binom{1}{0}
$$

- Multiplication with $X$

$$
X \cdot|\psi\rangle:=\left(\begin{array}{ll}
0 & 1 \\
1 & 0
\end{array}\right) \cdot\binom{1}{0}=\binom{0}{1}
$$



## Detour to linear algebra, cont'd

- Initialization into pure state

$$
|\psi\rangle=1 \cdot\binom{1}{0}+0 \cdot\binom{0}{1}=\binom{1}{0}
$$

- Multiplication with $X$

$$
X \cdot|\psi\rangle:=\left(\begin{array}{ll}
0 & 1 \\
1 & 0
\end{array}\right) \cdot\binom{1}{0}=\binom{0}{1}
$$

- Multiplication with $X$ once more

$$
X \cdot X \cdot|\psi\rangle:=\left(\begin{array}{ll}
0 & 1 \\
1 & 0
\end{array}\right) \cdot\binom{0}{1}=\binom{1}{0}
$$



## Detour to linear algebra, cont'd

- Initialization into pure state

$$
|\psi\rangle=1 \cdot\binom{1}{0}+0 \cdot\binom{0}{1}=\binom{1}{0}
$$

- Multiplication with another matrix

$$
H \cdot|\psi\rangle:=\frac{1}{\sqrt{2}}\left(\begin{array}{cc}
1 & 1 \\
1 & -1
\end{array}\right)\binom{1}{0}=\frac{1}{\sqrt{2}}\binom{1}{1}
$$



## Detour to linear algebra, cont'd

- Initialization into pure state

$$
|\psi\rangle=1 \cdot\binom{1}{0}+0 \cdot\binom{0}{1}=\binom{1}{0}
$$

- Multiplication with another matrix

$$
H \cdot|\psi\rangle:=\frac{1}{\sqrt{2}}\left(\begin{array}{cc}
1 & 1 \\
1 & -1
\end{array}\right)\binom{1}{0}=\frac{1}{\sqrt{2}}\binom{1}{1}
$$

- Double application of matrix $H$ gives

$$
H^{2} \cdot|\psi\rangle:=\frac{1}{\sqrt{2}}\left(\begin{array}{cc}
1 & 1 \\
1 & -1
\end{array}\right) \frac{1}{\sqrt{2}}\binom{1}{1}=\binom{1}{0}
$$



## Et voilà, our first quantum algorithm



## Quantum Inspire



| 1 | version 1.0 |
| :--- | :--- |
| 2 |  |
| 3 | qubits 1 |
| 4 | prep_z $\mathrm{q}[0]$ |
| 5 | $\mathrm{X} \mathrm{q}[0]$ |
| 6 | $\mathrm{H} \mathrm{q}[0]$ |
| 7 | $\mathrm{X} \mathrm{q}[0]$ |
| 8 | $\mathrm{H} \mathrm{q}[0]$ |
| 9 | measure $\mathrm{q}[0]$ |



## Detour to linear algebra, again

- Quantum gates can be expressed as unitary matrices
- $U \cdot U^{\dagger}=I=U^{\dagger} \cdot U$
- $\forall x \in \mathbb{C}^{n},\|U x\|=\|x\|$
- $\forall x, y \in \mathbb{C}^{n},\langle U x, U y\rangle=\langle x, y\rangle$
(quantum gates are reversible)
(length is preserved)
(inner product is preserved)
- Quantum algorithms can be expressed as chains of mat-vec multiplications

$$
\left|\psi_{\text {out }}\right\rangle=U_{d} \cdot U_{d-1} \cdot \ldots \cdot \underbrace{U_{2} \cdot \underbrace{U_{1} \cdot\left|\psi_{\text {in }}\right\rangle}_{\left|\psi^{\prime}\right\rangle}}_{\left|\psi^{\prime \prime}\right\rangle}=U \cdot\left|\psi_{\text {in }}\right\rangle
$$

## Reversible computing

- Quantum algorithms can be easily reversed (in theory!)

$$
\begin{aligned}
& U_{d}^{\dagger} \cdot\left|\psi_{\text {out }}\right\rangle=\underbrace{U_{d}^{\dagger} \cdot U_{d} \cdot U_{d-1} \cdot \ldots \cdot U_{2} \cdot U_{1} \cdot\left|\psi_{\text {in }}\right\rangle}_{I} \\
& U_{d-1}^{\dagger} \cdot U_{d}^{\dagger} \cdot\left|\psi_{\text {out }}\right\rangle=\underbrace{U_{d-1}^{\dagger} \cdot U_{d-1}}_{I} \cdot U_{d-2} \cdot \ldots \cdot U_{2} \cdot U_{1} \cdot\left|\psi_{\text {in }}\right\rangle \\
& U^{\dagger} \cdot\left|\psi_{\text {out }}\right\rangle=U_{1}^{\dagger} \cdot U_{2}^{\dagger} \cdot \ldots \cdot U_{d-1}^{\dagger} \cdot U_{d}^{\dagger} \cdot\left|\psi_{\text {out }}\right\rangle=\left|\psi_{\text {in }}\right\rangle
\end{aligned}
$$

- Many 'nice' mathematical properties
- unitary group $U(n)$
- unitary decomposition,...

Basic concepts of quantum computing

## QUANTUM REGISTERS

## Detour to linear algebra, yet again

- Tensor-product construction of single-qubit bases

$$
|0\rangle \otimes|0\rangle, \quad|0\rangle \otimes|1\rangle, \quad|1\rangle \otimes|0\rangle, \quad|1\rangle \otimes|1\rangle
$$

- Unique labelling of multi-qubit state

$$
\begin{aligned}
& |00\rangle=|0\rangle \otimes|0\rangle=\binom{1}{0} \otimes\binom{1}{0}=\left(\begin{array}{l}
1 \\
0 \\
0 \\
0
\end{array}\right) \\
& |01\rangle=|0\rangle \otimes|1\rangle=\binom{1}{0} \otimes\binom{0}{1}=\left(\begin{array}{l}
0 \\
1 \\
0 \\
0
\end{array}\right)
\end{aligned}
$$

## Multiple qubits



- Multi-qubit state

$$
\begin{aligned}
\left|\psi_{1} \psi_{2}\right\rangle & =\alpha_{0}|00\rangle+\alpha_{1}|01\rangle+\alpha_{2}|10\rangle+\alpha_{3}|11\rangle \\
& =\alpha_{0}\left(\begin{array}{l}
1 \\
0 \\
0 \\
0
\end{array}\right)+\alpha_{1}\left(\begin{array}{l}
0 \\
1 \\
0 \\
0
\end{array}\right)+\alpha_{2}\left(\begin{array}{l}
0 \\
0 \\
1 \\
0
\end{array}\right)+\alpha_{3}\left(\begin{array}{l}
0 \\
0 \\
1 \\
0
\end{array}\right)
\end{aligned}
$$

- such that

$$
\left|\alpha_{0}\right|^{2}+\left|\alpha_{1}\right|^{2}+\left|\alpha_{2}\right|^{2}+\left|\alpha_{3}\right|^{2}=1
$$

## Multiple qubits, cont'd



- Controlled-NOT gate

$$
\mathrm{CNOT}_{12}\left|\psi_{1} \psi_{2}\right\rangle=\left(\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1 \\
0 & 0 & 1 & 0
\end{array}\right)\left(\begin{array}{c}
\alpha_{0} \\
\alpha_{1} \\
\alpha_{2} \\
\alpha_{3}
\end{array}\right)=\left(\begin{array}{l}
\alpha_{0} \\
\alpha_{1} \\
\alpha_{3} \\
\alpha_{2}
\end{array}\right)
$$

- Outcome

$$
\begin{aligned}
& \alpha_{0}|00\rangle+\alpha_{1}|01\rangle+\alpha_{2}|10\rangle+\alpha_{3}|11\rangle \\
\mapsto & \alpha_{0}|00\rangle+\alpha_{1}|01\rangle+\alpha_{3}|10\rangle+\alpha_{2}|11\rangle \\
= & \alpha_{0}|00\rangle+\alpha_{1}|01\rangle+\alpha_{2}|11\rangle+\alpha_{3}|10\rangle
\end{aligned}
$$

## Zoo of quantum gates



$$
\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1 \\
0 & 0 & 1 & 0
\end{array}\right]
$$

$$
Y
$$

$$
\left[\begin{array}{llllllll}
1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\
0 & 0 & 0 & 0 & 0 & 0 & 1 & 0
\end{array}\right]
$$

$$
\left[\begin{array}{cc}
0 & -i \\
i & 0
\end{array}\right]
$$

$$
\begin{gathered}
T T \\
{\left[\begin{array}{cc}
1 & 0 \\
0 & e^{i \pi / 4}
\end{array}\right]}
\end{gathered}
$$

$\square$
$\left[\begin{array}{cc}1 & 0 \\ 0 & -1\end{array}\right]$

$$
\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

$$
\begin{aligned}
& -X \\
& {\left[\begin{array}{ll}
0 & 1 \\
1 & 0
\end{array}\right]} \\
& H \\
& \frac{1}{\sqrt{2}}\left[\begin{array}{cc}
1 & 1 \\
1 & -1
\end{array}\right] \\
& {\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & -1
\end{array}\right]} \\
& -2
\end{aligned}
$$

Basic concepts of quantum computing

## QUANTUM ALGORITHMS

## Example: 3-bit password



## Bell state

- $50: 50$ chance to measure $|0 ?\rangle$ or $|1 ?\rangle$
- But then we know the value of the second qubit without measurement since


$$
\left|\beta_{00}\right\rangle=\frac{1}{\sqrt{2}} \cdot|00\rangle+0 \cdot|01\rangle+0 \cdot|10\rangle+\frac{1}{\sqrt{2}} \cdot|11\rangle
$$



Quantum Teleportation


## Intermezzo: How difficult can it be to add two integers?



## Intermezzo: How difficult can it be to add two integers?



## A first quantum algorithm: 1+2=3



Carry Gate


Sum Gate

n extra ancilla qubits needed $(:)$

Cuccaro et al.: A new quantum ripple-carry addition circuit (2008)

## Another quantum algorithm: 1+2=3


M. vd. Lans: Quantum Algorithms and their Implementation on Quantum Computer Simulators, Master thesis, 2017

## Towards practical QC: $1+2 \cong 3$

1000 QX simulator runs with depolarizing noise error model

|  | 0,1 |  | $10^{-\frac{3}{2}}$ |  | 0,01 |  | $10^{-\frac{5}{2}}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.27045 | 0.3793 | 0.50545 | 0.2752 | 0.78965 | 0.1233 | 0.92285 | 0.0463 |
| 2 | 0.134061 | 0.221523 | 0.165182 | 0.209176 | 0.451353 | 0.134284 | 0.762621 | 0.0570876 |
| ᄃ 3 | 0.0601436 | 0.112097 | 0.0683512 | 0.116162 | 0.191802 | 0.105916 | 0.540766 | 0.0754021 |
| $\pm 4$ | 0.0336509 | 0.0611537 | 0.0351125 | 0.0589036 | 0.064375 | 0.0645881 | 0.306778 | 0.0802711 |
| ᄃ 5 |  |  |  |  | 0.0224336 | 0.031892 | 0.154869 | 0.0575671 |
| 回 6 |  |  |  |  | 0.00798384 | 0.0176539 | 0.0654961 | 0.033179 |
| 7 |  |  |  |  | 0.00398747 | 0.0076473 | 0.0252142 | 0.0167067 |
| 8 |  |  |  |  | 0.00254026 | 0.00363275 | 0.00834128 | 0.00823629 |

Standard circuit: prob. correct (left), largest prob. wrong answer (right)

Looman: Implementation and Analysis of an Algorithm on Positive Integer Addition for Quantum Computing (2018)

## Towards practical QC: $1+2 \cong 3$

1000 QX simulator runs with depolarizing noise error model


Optimized circuit: prob. correct (left), largest prob. wrong answer (right)

Looman: Implementation and Analysis of an Algorithm on Positive Integer Addition for Quantum Computing (2018)

Quantum-accelerated design optimization

## CONCEPTUAL FRAMEWORK

## Airfoil design



Double wedge airfoil (Supersonic)


## Simulation-based design and analysis cycle



## 1. Design $D(\boldsymbol{p})$



- Design parameters
- Admissible design space

$$
\boldsymbol{p}=\left(p_{1}, \ldots, p_{12}\right)
$$

$$
\mathcal{S}=\left[p_{1}^{\min }, p_{1}^{\max }\right] \times \cdots \times\left[p_{12}^{\min }, p_{12}^{\max }\right]
$$

## 2. Simulation

- Mathematical model

- Solution for one particular design

$$
U=U(D(\boldsymbol{p}))
$$



Linné FLOW Centre and SeRC, KTH, Sweden

## 3. Analysis

- Cost functional

$$
\mathcal{C}(U ; D)
$$




## Operation conditions



## Abstract design optimization

- Problem: Find a set of admissible design parameters $\boldsymbol{p}$ such that solution $U(D(\boldsymbol{p}))$ to the mathematical model $\mathcal{M}(U, D(\boldsymbol{p}))$ computed on the design $D(\boldsymbol{p})$ optimizes the cost functional $\mathcal{C}(U, D(\boldsymbol{p}))$ for fixed operation condition



## Academic model problem



## 4. Redesign

- Problem: Minimize the difference

$$
d_{h}=u_{h}-u_{h}^{*}
$$

between the solution $u_{h}$ and a given profile $u_{h}^{*}$ w.r.t.
3. Analysis

$$
\mathcal{C}\left(d_{h}, p\right)=d_{h}^{T} M d_{h}
$$

such that $d_{h}$ solves

$$
A_{h} d_{h}=f_{h}-A_{h} u_{h}^{*}
$$

## Quantum acceleration

- Best classical solution algorithm
$\mathcal{O}($ Nsк $\log (1 / \epsilon))$
- Quantum Linear Solver Algorithm
- HHL: $\mathcal{O}\left(\log (N) s^{2} \kappa^{2} / \epsilon\right)$
- Ambainis: $\mathcal{O}\left(\log (N) s^{2} \kappa / \epsilon\right)$


## Quantum acceleration

- Best classical solution algorithm

$$
\mathcal{O}(N s \kappa \log (1 / \epsilon))
$$

- Quantum Linear Solver Algorithm
- HHL: $\mathcal{O}\left(\log (N) s^{2} \kappa^{2} / \epsilon\right)$
- Ambainis: $\mathcal{O}\left(\log (N) s^{2} \kappa / \epsilon\right)$
- Quadratic form optimizer
$\mathcal{O}\left((\# \text { design parameters })^{2}\right)$
- Jordan's QOPT
$\mathcal{O}\left((\# \text { design parameters })^{1}\right)$


## Quantum speed-up



## Quantum speed-up (?)



## Quantum speed-up (?)

Rigetti 128
Google 72


Practical aspects of quantum computing

## SDKS AND GOOD PRACTICES

## How accelerated computing works



How accelerated computing works


Accelerator



## How accelerated computing works



## How accelerated computing works



## How accelerated computing works



## How accelerated computing works



## How accelerated computing works



## It feels like GPU-computing in the early 2000

- Quantum languages
- AQASM: Atos QML
- cQASM: QuTech QX, TNO QI
- OpenQASM: IBM, Google
- Quil: Rigetti
- ...
- Quantum SDKs
- pyAqasm
- pyQuil
- Circ
- OpenQL/QX
- ProjectQ
- QisKit
- Quantum Development Kit
- Quirk
- ...


## It feels like GPU-computing in the early 2000

| Algorithm | pyQuil | Qiskit | ProjectQ | QDK |
| :---: | :---: | :---: | :---: | :---: |
| Random Generator | $\checkmark$ (T) | $\checkmark$ ( T$)$ | $\checkmark$ (T) | $\checkmark$ (T) |
| Teleportation | $\checkmark$ (T) | $\checkmark$ (T) | $\checkmark$ (T) | $\checkmark$ (T) |
| Swap Test | $\checkmark$ (T) |  |  |  |
| Deutsch-Jozsa | $\checkmark$ (T) | $\checkmark$ (T) |  | $\checkmark$ (T) |
| Grover's | $\checkmark$ (T) | $\checkmark$ ( T ) | $\checkmark$ (T) | $\checkmark$ (B) |
| Quantum <br> Fourier <br> Transform | $\checkmark$ (T) | $\checkmark$ (T) | $\checkmark$ (B) | $\checkmark$ (B) |
| Shor's Algorithm |  |  | $\checkmark$ (T) | $\checkmark$ (D) |
| Bernstein Vazirani | $\checkmark$ (T) | $\checkmark$ (T) |  | $\checkmark$ (T) |
| Phase Estimation | $\checkmark$ (T) | $\checkmark$ (T) |  | $\checkmark$ (B) |
| $\begin{aligned} & \text { Optimization/ } \\ & \text { QAOA } \\ & \hline \end{aligned}$ | $\checkmark$ (T) | $\checkmark$ (T) |  |  |
| $\begin{aligned} & \text { Simon's } \\ & \text { Algorithm } \\ & \hline \end{aligned}$ | $\checkmark$ (T) | $\checkmark$ ( T ) |  |  |
| Variational <br> Quantum Eigensolver | $\checkmark$ (T) | $\checkmark$ (T) | $\checkmark$ ( P ) |  |
| Amplitude Amplification | $\checkmark$ (T) |  |  | $\checkmark$ (B) |
| Quantum Walks |  | $\checkmark$ (T) |  |  |
| Ising Solver | $\checkmark$ (T) |  |  | $\checkmark$ (T) |
| Quantum Gradient Descent | $\checkmark$ (T) |  |  |  |
| Five $\quad$ Qubit Code |  |  |  | $\checkmark$ (B) |
| Repetition Code |  | $\checkmark$ (T) |  |  |
| Steane Code |  |  |  | $\checkmark$ (B) |
| Draper Adder |  |  | $\checkmark$ (T) | $\checkmark$ (D) |
| Beauregard Adder |  |  | $\checkmark$ (T) | $\checkmark$ (D) |
| Arithmetic |  |  | $\checkmark$ (B) | $\checkmark$ (D) |
| $\begin{aligned} & \hline \text { Fermion } \\ & \text { Transforms } \end{aligned}$ | $\checkmark$ (T) | $\checkmark$ (T) | $\checkmark$ (P) |  |
| Trotter Simulation |  |  |  | $\checkmark$ (D) |
| Electronic Structure (FCI, $\quad$ MP2, HF, etc.) |  |  | $\checkmark$ ( P ) |  |
| $\begin{aligned} & \text { Process } \\ & \text { Tomography } \\ & \hline \end{aligned}$ | $\checkmark$ (T) | $\checkmark$ (T) |  | $\checkmark$ (D) |
| $\begin{aligned} & \text { Vaidman De- } \\ & \text { tection Test } \\ & \hline \end{aligned}$ |  | $\checkmark$ ( T ) |  |  |



## |LIB): Kwantum expression template LIBrary

- Header-only C++14 library
- Open-source release by summer
- Auto-generation of quantum code from C++ expression templates
- Bi-directional communication between host and quantum device
- Made for quantum-accelerated scientific computing



## |LIB〉: Kwantum expression template LIBrary

```
auto expr = measure(h(x(h(x(init())))));
```

Qdata<1, OpenQASMv2> backend;
json result = expr(backend).execute();

```
QInt<3> a(1);
QInt<3> b(2);
a += b;
```


## Conclusion

- Quantum computers have huge potential as special-purpose accelerators to speed-up the solution of (mathematical) problems 'exponentially'
- Convergence towards common quantum programming language and development toolchain needed to make end-users interested (if at all!)
- To fully exploit the power of quantum computers don't mimic classical algorithms but redesign quantum algorithms from scratch based on quantum-mechanical principles like superposition and entanglement

Thank you very much!

